

Population and Welfare: The Greatest Good for the Greatest Number

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Motivation

- Economic growth is typically measured in **per capita** terms
 - Puts **zero** weight on having more people – extreme!
- *Hypothetical*: Two countries with same TFP_t . One has constant N but rising c , the other has constant c but rising N .
 - **Example**: Japan is 6x richer p.c. than in 1960, while Mexico is 3x richer
But Mexico's population is 3x larger than in 1960 vs. 1.3x for Japan
 - **Example**: Population growth over thousands of years
- **Key Question**:
How much has population growth contributed to aggregate welfare growth?

Examples of how this could be useful

- The Black Death, HIV/AIDS, or Covid-19
- China's one-child policy
- What fraction of GDP should we spend to mitigate climate change in 2100?
 - How many people today versus in the year 2100?
- How much to spend to avoid existential risks (asteroids, nuclear war)?
 - Many billions of people-years in the future

What we're *not* doing

- We use the MRS in aggregate welfare between people N and per capita c
- Answering other key questions would require the social MRT from the production side (externalities from ideas, human capital, pollution)
 - Optimal fertility?
 - Was the demographic transition good or bad?
- Our approach is just accounting with total welfare – need fewer assumptions

Outline

- **Part I.** Baseline calculation with only population and consumption
- **Part II.** Adjusting for migration (who gets credit?)
- **Part III.** Incorporating parental altruism and endogenous fertility



Part I. Baseline calculation
with only population and consumption

Flow Aggregate Welfare

- Setup
 - c_t consumption per person
 - $u(c_t) \geq 0$ is flow of utility enjoyed by each person
 - N_t identical people
- Summing over people \Rightarrow aggregate utility flow

$$W(N_t, c_t) = N_t \cdot u(c_t)$$

- Non-existence is valued at zero
- Assumes “utility when not born” = “utility when dead”

Total utilitarianism

- Critiques
 - Repugnant conclusion (Parfit, 1984)
 - Inalienable rights
- Versus per capita utilitarianism
 - e.g. Jones and Klenow (2016)
 - Sadistic conclusion
- Zuber et al. (2020), De la Croix and Doepke (2021), MacAskill (2022)

Growth in consumption-equivalent aggregate welfare

$$\frac{dW_t}{W_t} = \frac{dN_t}{N_t} + \frac{u'(c_t)c_t}{u(c_t)} \cdot \frac{dc_t}{c_t}$$

$$\underbrace{\frac{u(c_t)}{u'(c_t)c_t} \cdot \frac{dW_t}{W_t}}_{\text{CE-Welfare growth}} = \underbrace{\frac{u(c_t)}{u'(c_t)c_t} \cdot \frac{dN_t}{N_t}}_{\equiv v(c_t)} + \frac{dc_t}{c_t}$$

- $v(c)$ = value of having one more person live for a year
 - expressed relative to one year of per capita consumption
- 1 pp of population growth is worth $v(c)$ pp of consumption growth

Calibrating $v(c)$ in the U.S. in 2006

- Using the EPA's VSL of \$7.4m in 2006:

$$v(c) \equiv \frac{u(c)}{u'(c) \cdot c} = \frac{\text{VSLY}}{c} \approx \frac{\text{VSL}/e_{40}}{c} \approx \frac{\$7,400,000/40}{\$38,000} = \frac{\$185,000}{\$38,000} \approx 4.87$$

- 1 pp population growth is worth ~ 5 pp consumption growth

Measuring $v(c)$ in other years and countries

- Baseline: Assume $u(c) = \bar{u} + \log c$

$$v(c) \equiv \frac{u(c)}{u'(c) \cdot c} = u(c) = \bar{u} + \log c$$

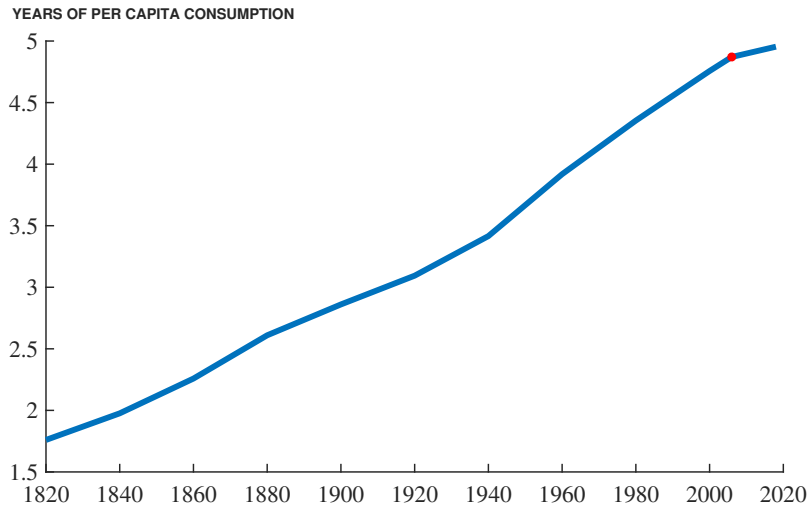
Higher consumption raises the value of a year of life

- Calibration:
 - Normalize units so that $c_{2006, US} = 1$
 - Then $v(c_{2006, US}) = 4.87$ implies $\bar{u} = 4.87$

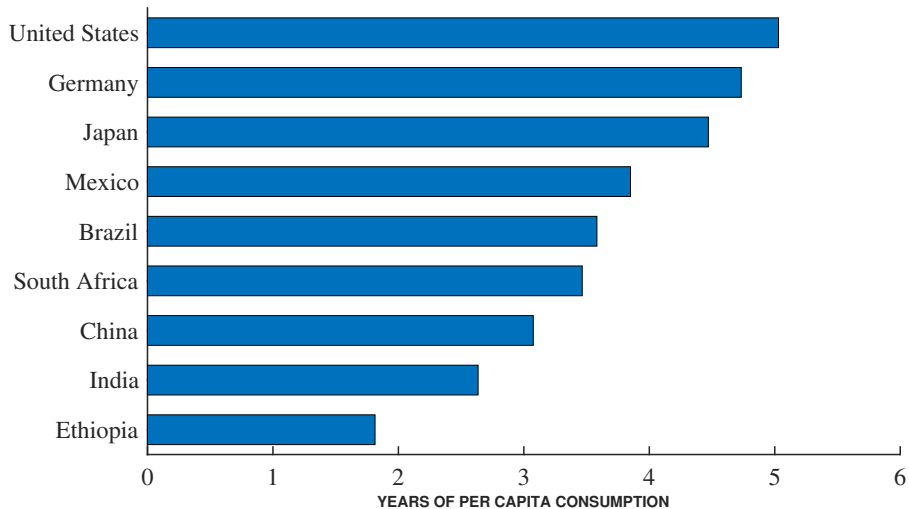
Alternative calibrations of \bar{u}

- Baseline assumes $v(c_{2006,US}) = 4.87 \rightarrow \bar{u} = 4.87$ when normalize $c_{2006,US} = 1$
- Consider values from meta studies by Viscusi (1993), Viscusi and Aldy (2003)
 - Based on U.S. labor-market risks and expressed in \$USD for 2000
- Median across all studies they discuss is \$5 million
 - Assume 40 years of life expectancy, year 2000 consumption of \$29,000
 - Yields $v(c_{2000,US}) = 4.30 \rightarrow \bar{u} = 4.44$ when $c_{2006,US} = 1$
- Median across their set of *preferred* studies is \$7 million
 - Yields $v(c_{2000,US}) = 6.02 \rightarrow \bar{u} = 6.16$ when $c_{2006,US} = 1$

$v(c)$ over time in the U.S.



$v(c)$ across countries in 2019



Recap

$$g_{\lambda} = v(c) \cdot g_N + g_c$$

λ is consumption-equivalent welfare

g_N is population growth

g_c is the growth rate of per capita consumption

- If $v(c) = 1$, then CE-Welfare growth is just aggregate consumption growth
- But $v(c) = 3$ or 5 implies much larger weight on population growth

Baseline samples

Penn World Tables 10.0

Years	# of OECD countries	# of non-OECD countries
1960-2019	38	63

Maddison (2020), BEA, Barro and Ursua (2008)

Years	Sample
1840-2018	United States
1850-2018	The “West”
1500-2018	The World

Overview of baseline results for 101 countries from 1960 to 2019

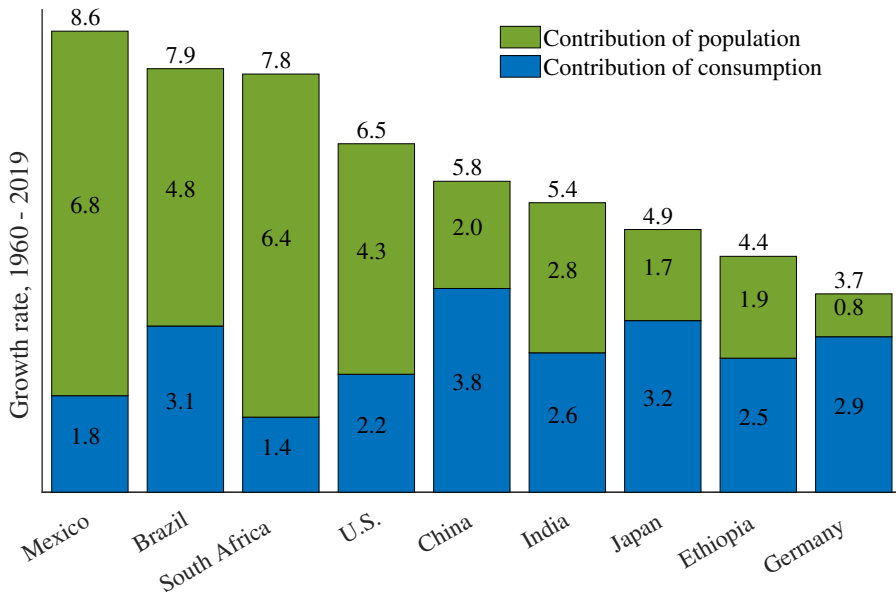
Average $g_c = 2.1\%$ and average $g_N = 1.8\%$ across the 101 countries

	Baseline	— Robustness —	
	$\bar{u} = 4.87$	$\bar{u} = 4.44$	$\bar{u} = 6.16$
CE-Welfare Growth	6.2%	5.4%	8.5%
Contribution of population	4.1%	3.3%	6.4%
Average value of life $v(c)$	2.7	2.3	4.0
Pop Share of CE-Welfare Growth	66%	63%	73%
Pop Share (if weight by population)	51%	46%	62%
# of countries with pop share $\geq 50\%$	78	69	89

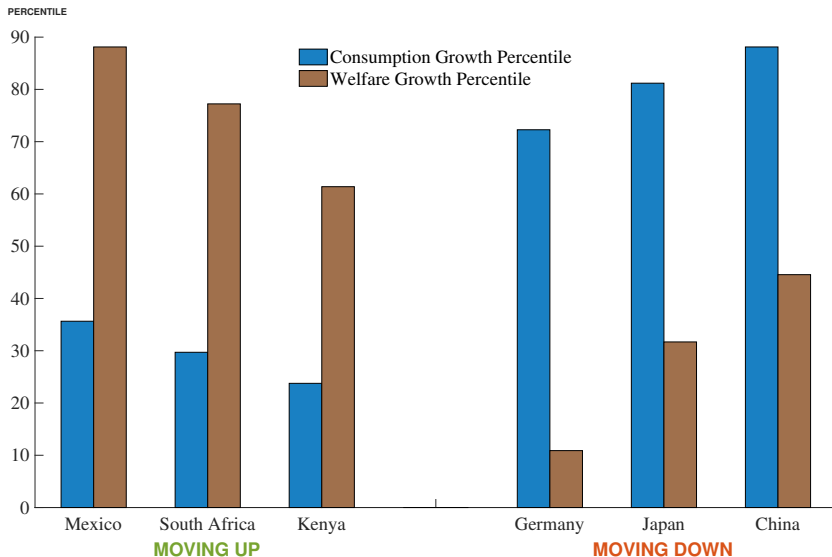
Decomposing welfare growth in select countries, 1960–2019

	g_λ	g_c	g_N	$v(c)$	$v(c) \cdot g_N$	Pop Share
Mexico	8.6	1.8	2.1	3.4	6.8	79%
Brazil	7.9	3.1	1.8	2.8	4.8	61%
South Africa	7.9	1.4	2.1	3.1	6.4	82%
United States	6.5	2.2	1.0	4.4	4.3	66%
China	5.7	3.8	1.3	1.8	2.0	34%
India	5.3	2.6	1.9	1.6	2.8	52%
Japan	4.9	3.2	0.5	3.8	1.7	34%
Ethiopia	4.4	2.5	2.7	0.7	1.9	44%
Germany	3.8	2.9	0.2	4.0	0.8	22%

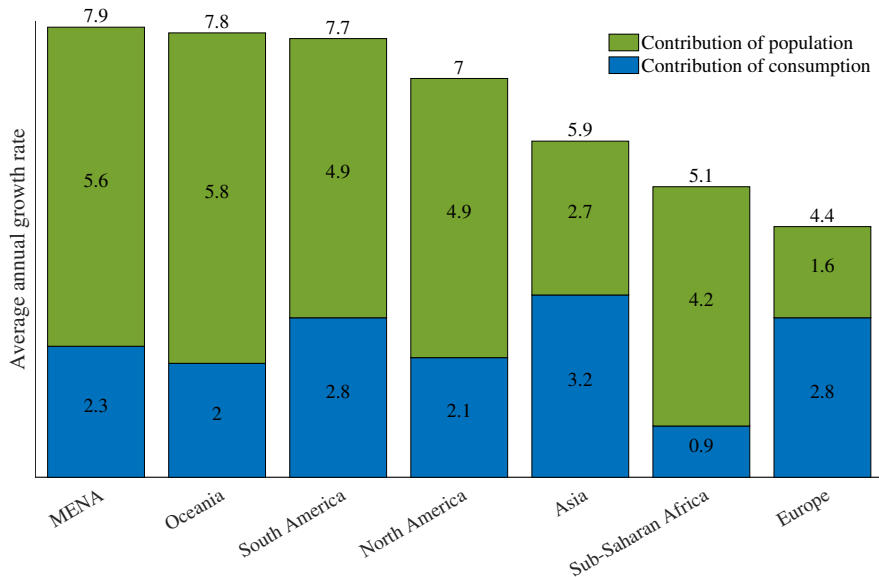
Average CE welfare growth for select countries, 1960–2019



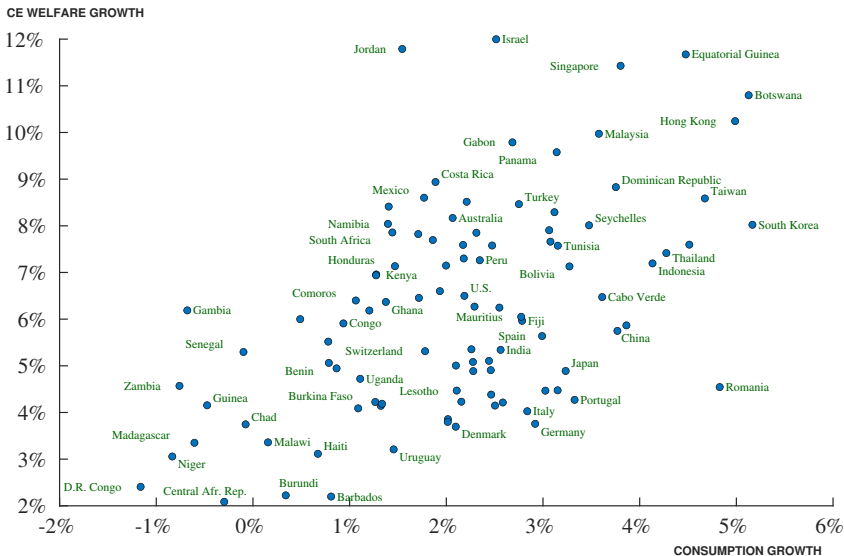
Some big differences in percentiles, 1960–2019 growth



Average CE welfare growth by region, 1960–2019

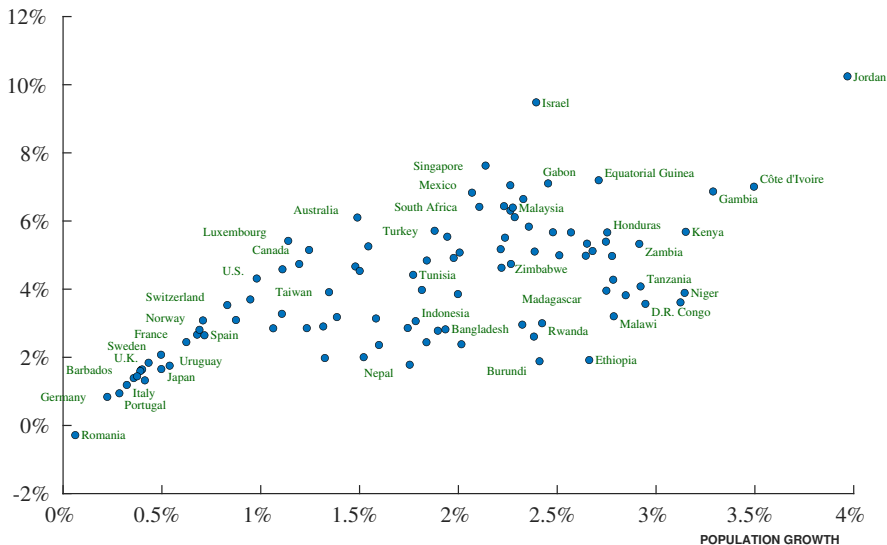


Plot of CE-Welfare growth against consumption growth, 1960-2019

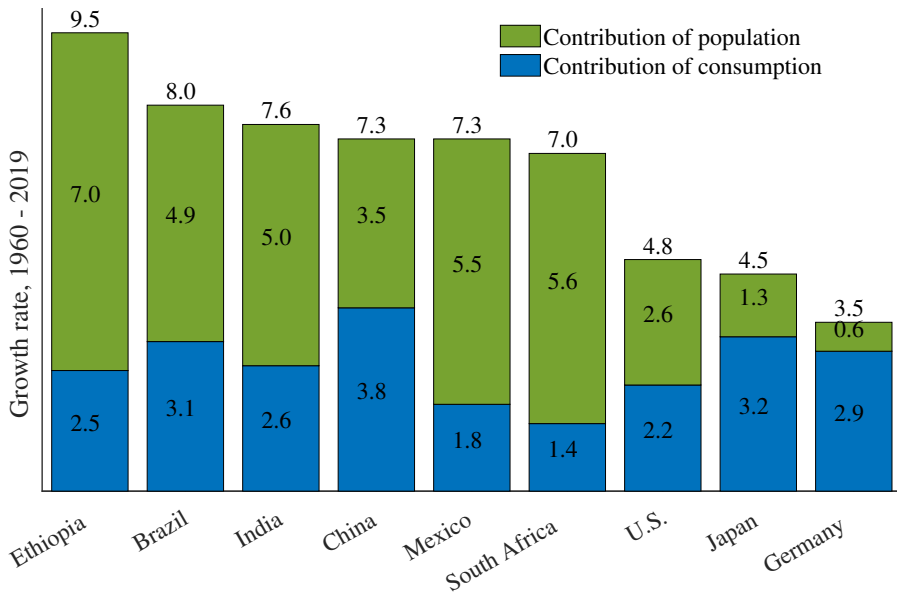


Contribution of Population Growth

POPULATION TERM IN CEWGROWTH



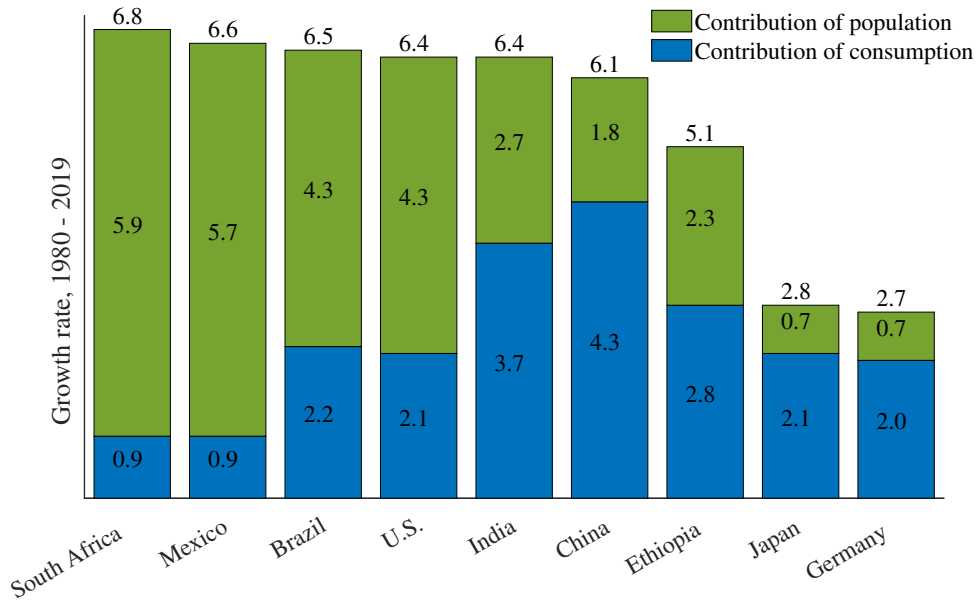
Robustness to constant $v(c) = 2.7$, 1960–2019



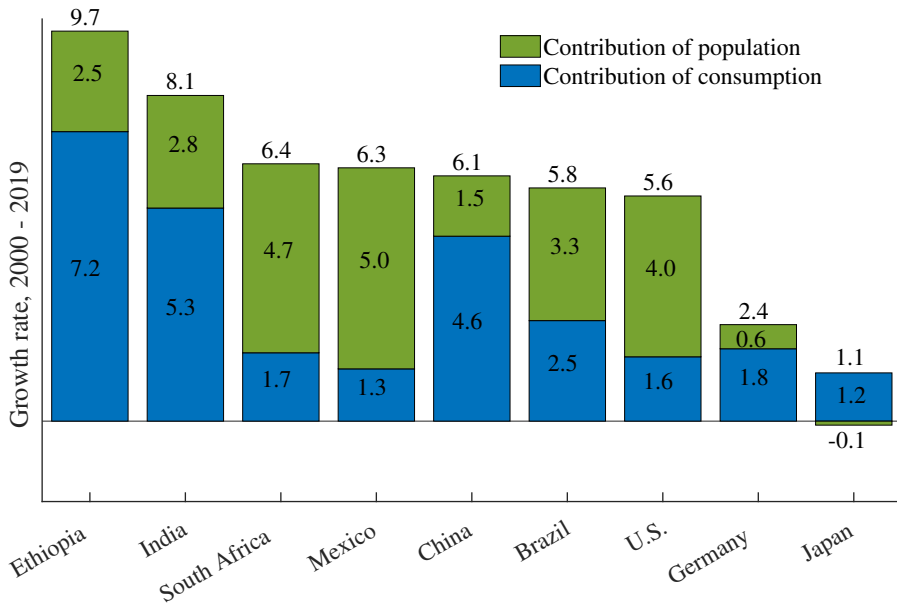
Scatterplot with constant $v(c) = 2.7$, 1960-2019



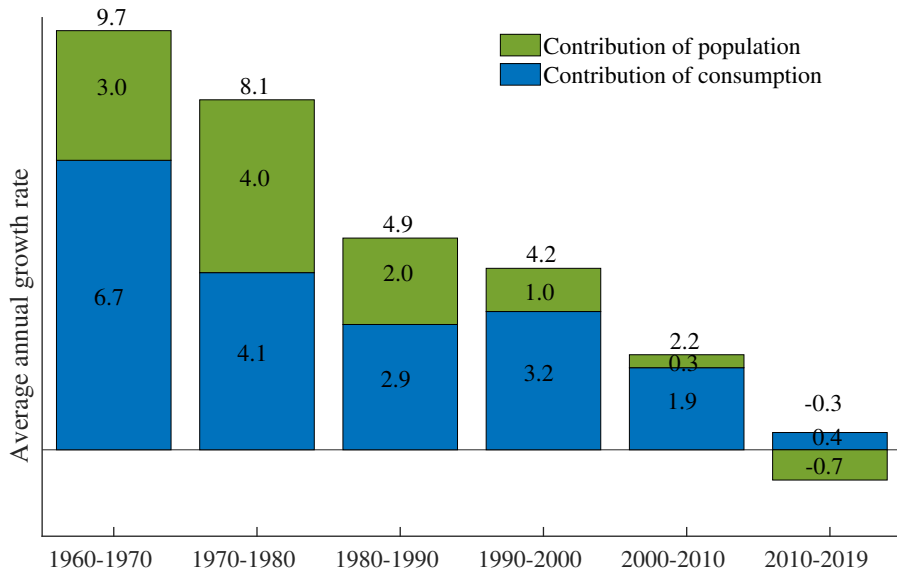
Average CE welfare growth for select countries, only for 1980–2019



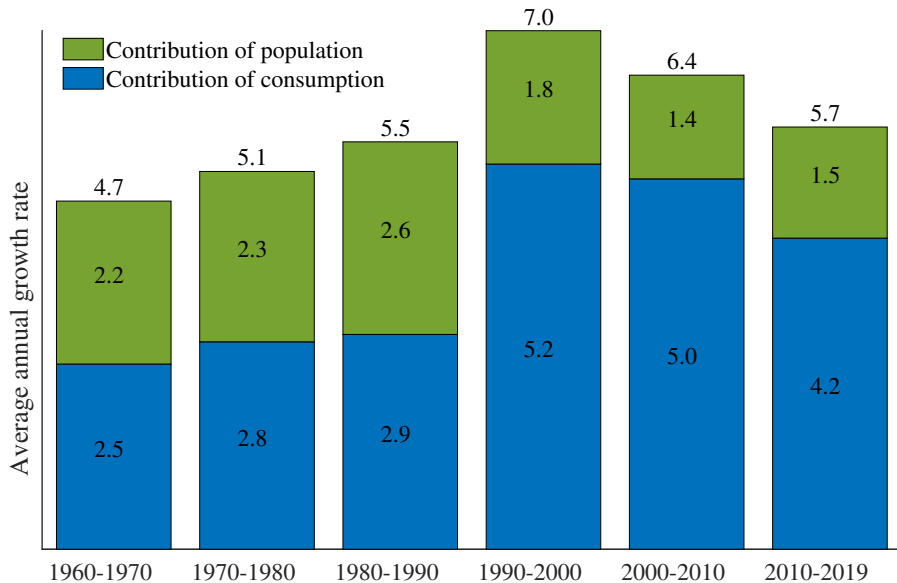
Average CE welfare growth for select countries, only for 2000–2019



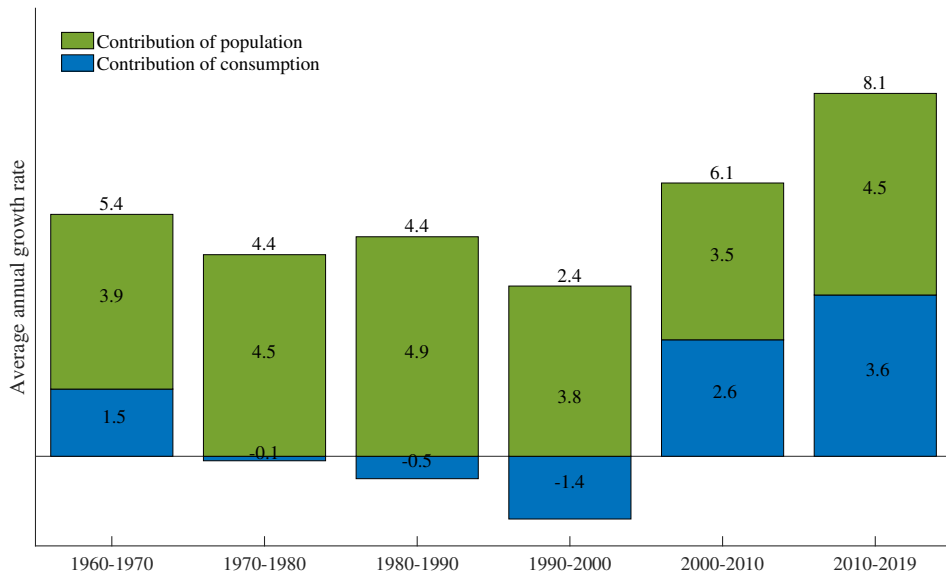
Average annual growth in Japan



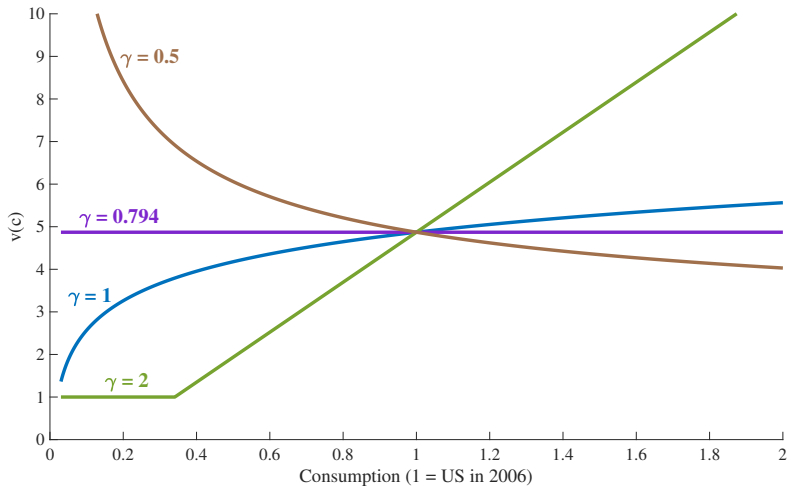
Average annual growth in China



Average annual growth in Sub-Saharan Africa



$v(c)$ for different values of γ



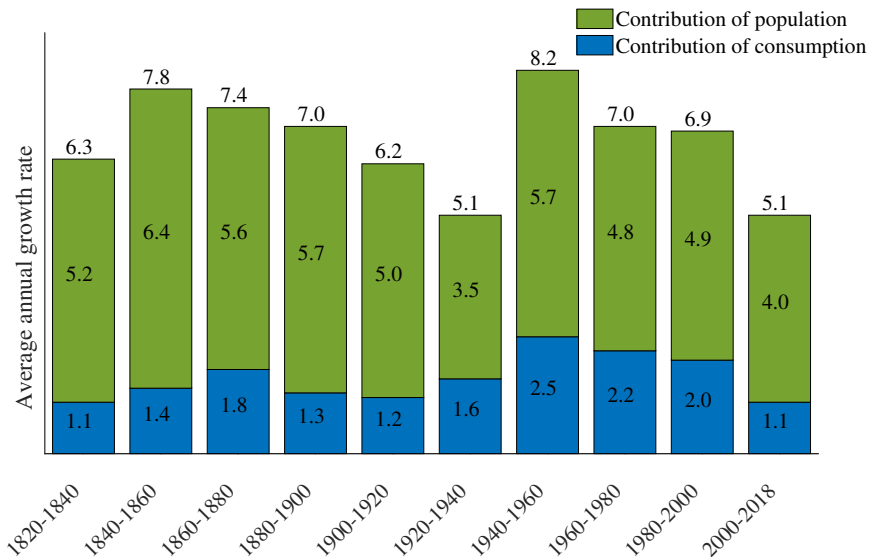
Weight on population growth is very high, either in past or future or both!

Robustness to alternative values of γ

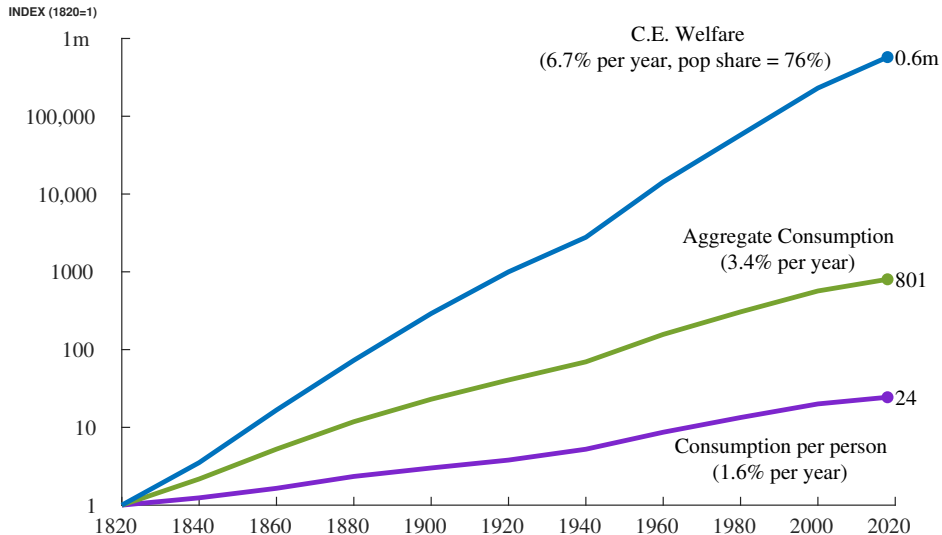
	$\gamma = 1$	$\gamma = 2$	$\gamma = 0.794$
CE-Welfare Growth	6.2%	4.2%	10.9%
Contribution of population	4.1%	2.1%	8.8%
Average value of life $v(c)$	2.7	1.3	4.9
Pop Share of CE-Welfare Growth	66%	53%	76%
Pop Share (if weight by population)	51%	40%	70%
# of countries with pop share $\geq 50\%$	78	47	90

Notes: In our calibration, when $\gamma = 0.794$, $v = 4.87$ for all country-years.

Trends over the long run for the U.S. (1820–2018)



U.S. cumulative growth, 1820–2018



Roles of birth and death rates

- Using estimates that value longevity, but not for being born
- For 24 countries calculate contributions longevity vs. fertility on pop. growth
 - Consider thought experiment of no decline in death rates
- Fertility contributes three quarters of population growth

Counterfactual: no decline in mortality

$$N_a(t) = \begin{cases} N_{a-1}(t-1) + M_a(t) - D_a(t) = \frac{N_{a-1}(t-1) + M_a(t)}{1 + d_a(t)} & \text{if } a > 0 \\ B(t) + M_a(t) - D_a(t) = \frac{B(t) + M_a(t)}{1 + d_a(t)} & \text{if } a = 0 \end{cases}$$

where $M_a(t)$ = age a net migration in year t ; $B(t)$ = births in year t

$D_a(t) = d_a(t) \cdot N_a(t)$ = age a deaths in year t

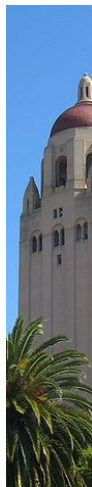
Counterfactual: fix death rates d_a 's at 1960 levels, but B and M_a as in data

Data: From Human Mortality Database for $N_a(t)$, $D_a(t)$ and $B(t)$ for 24 countries

- Australia, Austria, Belgium, Canada, Czechia, Denmark, Finland, France, Luxembourg, Norway, Spain, UK, Italy, Japan, Netherlands, Sweden, Switzerland, Iceland, USA, Portugal, Israel (1983 forward), Hong Kong (1986 forward), Croatia (2001 forward), Korea (2003 forward)

Relative importance of fertility for pop. growth for the 24 countries

5 select countries	g_N	Counterfactual g_N
France	0.6%	0.4%
UK	0.4%	0.2%
Italy	0.3%	0.1%
Japan	0.5%	0.1%
USA	1.0%	0.9%
All countries – pop. weighted	0.72%	0.53%

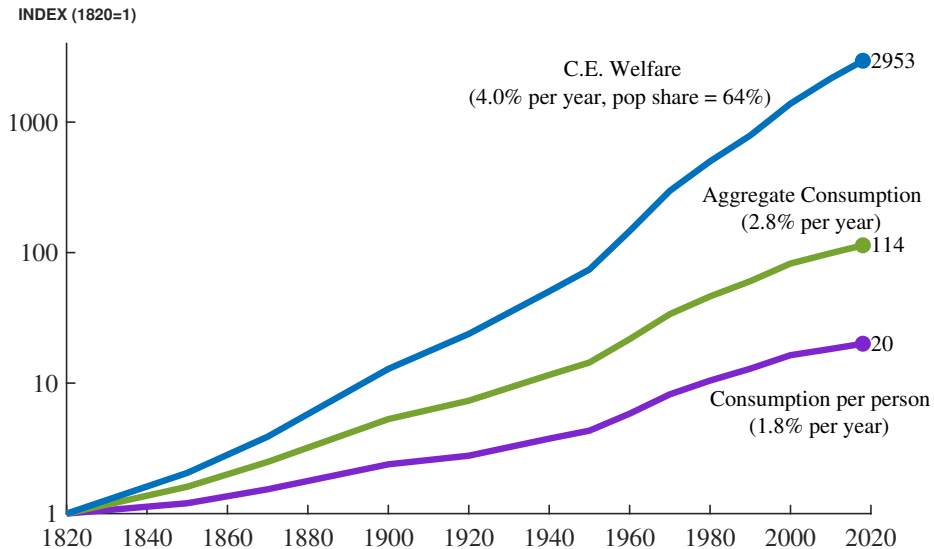


Part II. Adjusting for migration

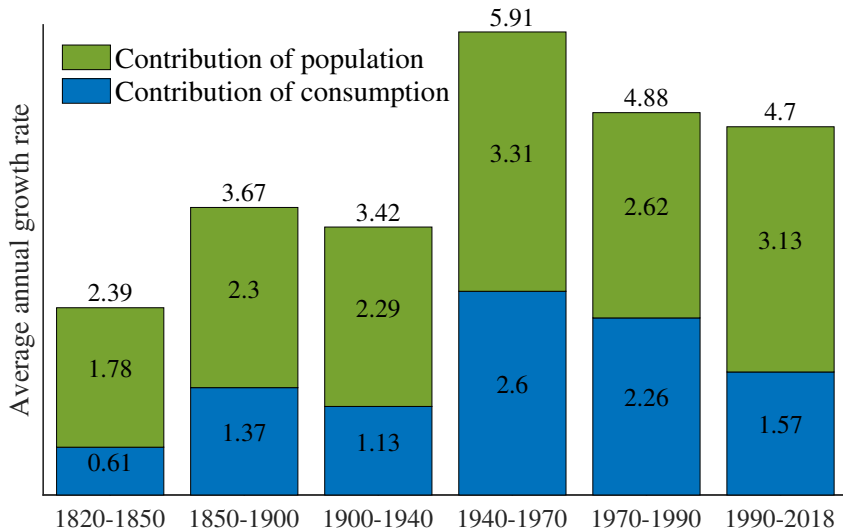
Aggregation to deal with immigration

- Should countries receive “credit” for population growth from immigration?
- Affects the Western Hemisphere vs. Europe in past century-plus
- Looking at “The West” as a whole should mitigate this problem
 - Includes Western Europe, U.S., Canada, Australia, New Zealand
- We do so back to 1820 to encompass the Age of Mass Migration

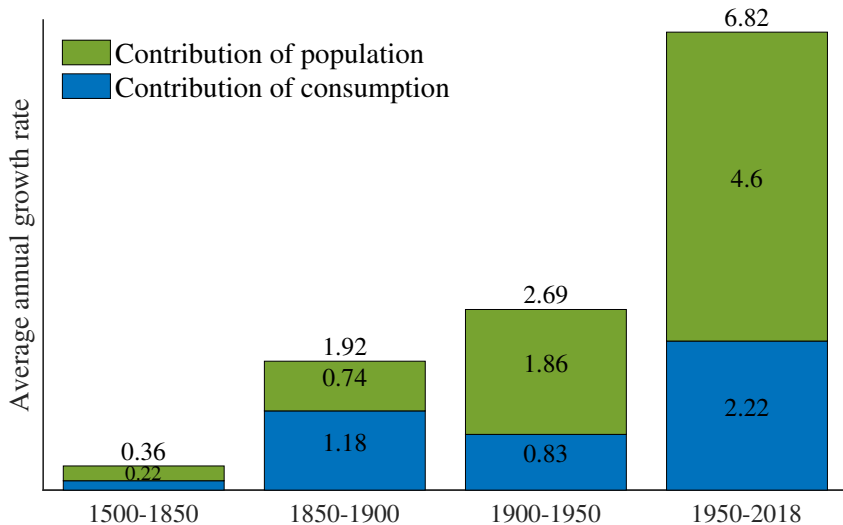
Cumulative growth in “The West”, 1820–2018



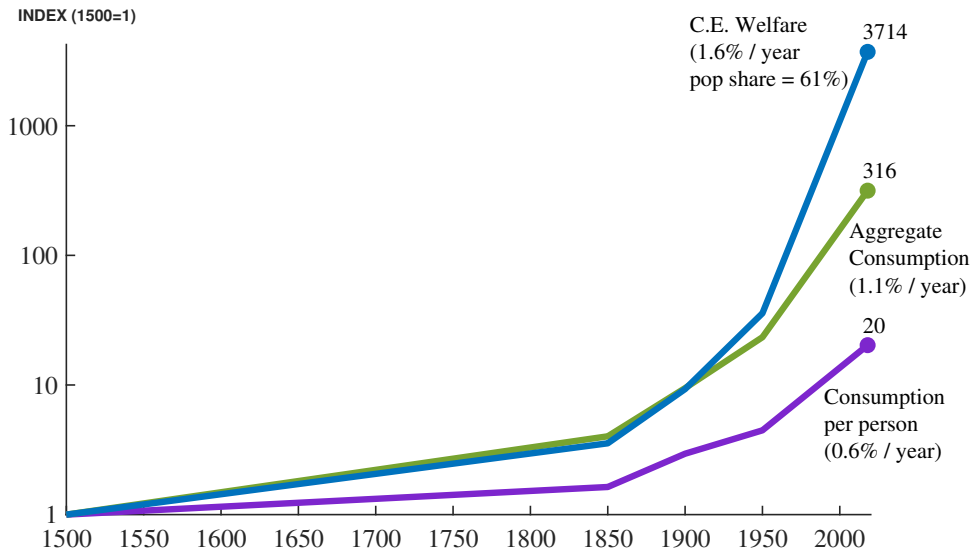
West CE-Welfare growth over the long run, 1820-2018



World CE-Welfare growth over the long run, 1500-2018



World cumulative growth, 1500-2018



Adjusting *country* welfare for migration

$$W_{it} = N_{it} \cdot u(c_{it}) + \sum_{j \neq i} N_{i \rightarrow j,t} \cdot u(c_{jt}) - \sum_{j \neq i} N_{j \rightarrow i,t} \cdot u(c_{it})$$

- $N_{i \rightarrow j,t}$ = population born in country i , living in country j in year t
- $N_{j \rightarrow i,t}$ = population born in country j , living in country i in year t
- Could also explore intermediate cases

Growth in country welfare adjusted for migration

$$\begin{aligned} g_{\lambda_{it}} &= v(c_{it}) \cdot g_{N_{it}} + g_{c_{it}} \\ &+ \sum_{j \neq i} \frac{N_{i \rightarrow j,t}}{N_{it}} \cdot \frac{u(c_{jt})}{u(c_{it})} \left(v(c_{it}) \cdot g_{N_{i \rightarrow j,t}} + \frac{v(c_{it})}{v(c_{jt})} \cdot g_{c_{jt}} \right) \\ &- \sum_{j \neq i} \frac{N_{j \rightarrow i,t}}{N_{it}} \left(v(c_{it}) \cdot g_{N_{j \rightarrow i,t}} + g_{c_{it}} \right) \end{aligned}$$

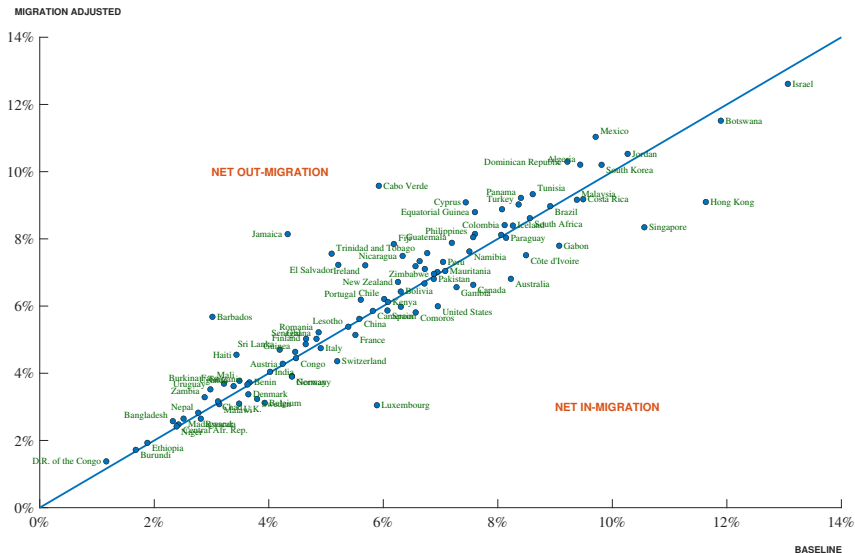
- Our baseline credits all immigrants to **destination** country
- Migration adjustment credits them to **source** country instead

Summary of migration results

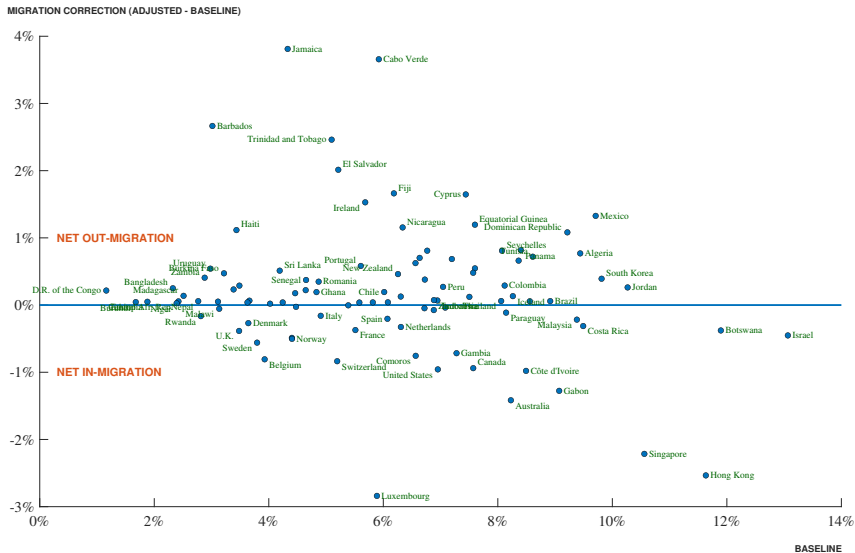
- Have the necessary data for 81 countries from 1960 to 2000
- Results with and without the migration adjustment highly correlated at 0.92
- But the adjustments for individual countries can be large ~ 2 pp
- Average absolute adjustment is 0.6pp

Source: The World Bank's Global Bilateral Migration Database

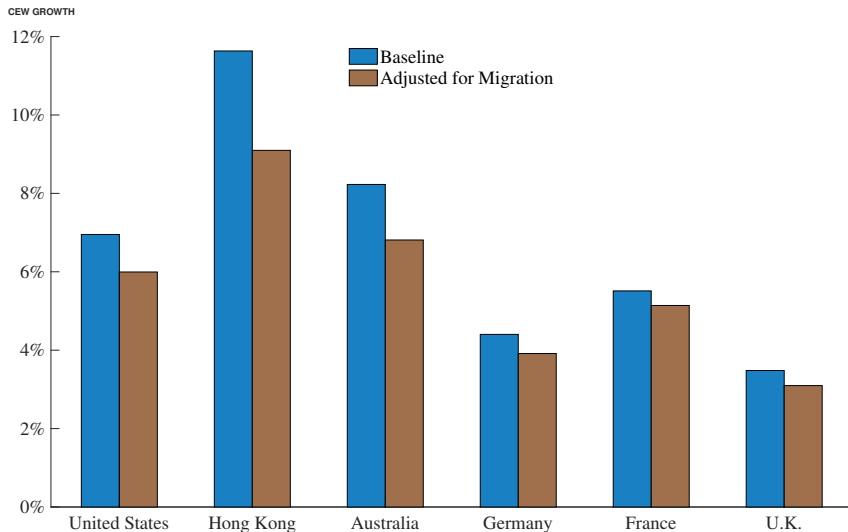
Baseline vs. Migration-Adjusted CEW growth



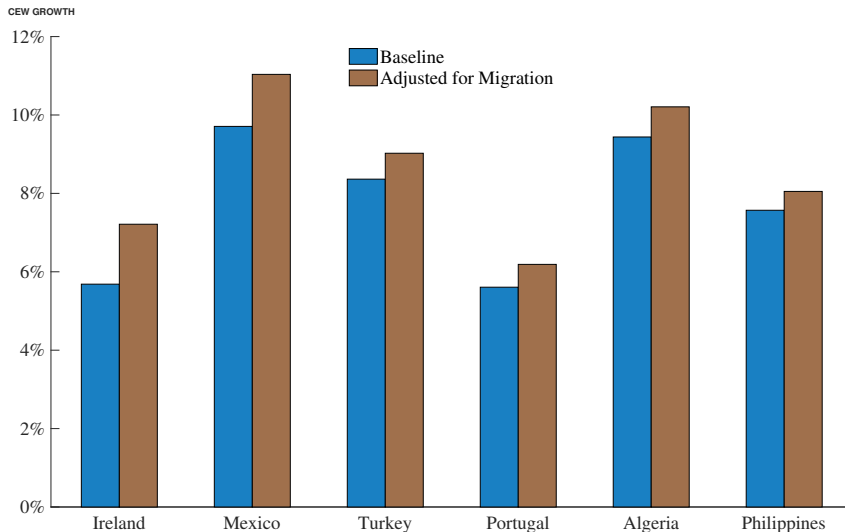
Migration correction vs Baseline CEW growth



Countries for which in-migration biases our baseline upward



Countries for which out-migration biases our baseline downward





Part III. Parental altruism and endogenous fertility
a la Barro-Becker (1989)

Parental altruism and fertility

- Parents have kids because they love them – missing in our baseline
 - Account for reduced fertility on parental welfare (Cordoba, 2015)
- But falling fertility may be compensated by higher per capita utility:
 - Quantity / quality trade-off \implies fewer but “better” kids
- Accordingly, extend framework to incorporate:
 - Broader measure of flow utility, including quantity/quality of kids
 - *Privately* optimal fertility, consumption, and time use by parents

Flow aggregate welfare

$$W(N_t^p, N_t^k, c_t, l_t, c_t^k, h_t^k, b_t) = N_t^p \cdot u(c_t, l_t, c_t^k, h_t^k, b_t) + N_t^k \cdot \tilde{u}(c_t^k)$$

- N^p = number of adults
 - N^k = number of children
 - b = number of children per adult
 - c = adult consumption
 - l = adult leisure
 - c^k = child consumption
 - h^k = child human capital
- $$\implies N = N^p + N^k = (1 + b) \cdot N^p$$

Consumption equivalent welfare:

$$W(N_t^p, N_t^k, \lambda_t \cdot c_t, l_t, \lambda_t \cdot c_t^k, h_t^k, b_t) = W(N_{t+dt}^p, N_{t+dt}^k, c_{t+dt}, l_{t+dt}, c_{t+dt}^k, h_{t+dt}^k, b_{t+dt})$$

Parental utility maximization problem

$$\max_{c, l, c^k, h^k, b} u(c_t, l_t, c_t^k, h_t^k, b_t)$$

$$\text{subject to: } c_t + b_t \cdot c_t^k \leq w_t \cdot h_t \cdot l_{ct}$$

$$h_t^k = f_t(h_t \cdot e_t) \quad \text{and} \quad l_{ct} + l_t + b_t \cdot e_t \leq 1$$

- w = wage per unit of human capital
- h = parental human capital, equals inherited h^k
- l_c = parental hours worked
- e = parental time investment per child

Parents' vs. Kids' Consumption

- Make two assumptions on preferences:
 - *Assumption 1:* $u(c_t^p, c_t^k, \vec{x}_t) = \log(c_t^p) + \alpha b_t^\theta \log(c_t^k) + g(l_t, b_t, h_t^k)$
 - *Assumption 2:* $\tilde{u}(c^k) = \bar{u}_k + \log(c_t^k)$
- With these assumptions: $\frac{c_t^k}{c_t^p} = \alpha b_t^{\theta-1}$
 - For $\theta < 1$, $\frac{c_t^k}{c_t^p}$ falls with b_t
 - Conditional on calibrating α and θ , do not need data on trends in $\frac{c_t^k}{c_t^p}$

Consumption-equivalent welfare growth

$$g_{\lambda_t} = \text{pop_term}_t$$

$$+ \pi_t^p \cdot \left(\frac{dc_t^p}{c_t^p} + \frac{u_{l_t} l_t}{u_{c_t} c_t} \cdot \frac{dl_t}{l_t} + \frac{u_{h_t^k} h_t^k}{u_{c_t} c_t} \cdot \frac{dh_t^k}{h_t^k} + \frac{u_{b_t} b_t}{u_{c_t} c_t} \cdot \frac{db_t}{b_t} \right) + (1 - \pi_t^p) \cdot \frac{dc_t^k}{c_t^k},$$

where $\pi_t^p = \frac{N_t^p}{(1 + \alpha b_t^\theta) N_t^p + N_t^k}$

$$\text{pop_term}_t = \frac{1 + b_t}{1 + \alpha b_t^\theta + b_t} \left[\frac{N_t^p}{N_t^k + N_t^p} \cdot \frac{dN_t^p}{N_t^p} \cdot v(c_t^p, \dots) + \frac{N_t^k}{N_t^k + N_t^p} \cdot \frac{dN_t^k}{N_t^k} \cdot \tilde{v}(c_t^k) \right]$$

Two differences in the population term relative to baseline calculation:

- ① Not imposing $\tilde{v}(c_t^k) = v(c_t, \dots)$
- ② Altruism term $\alpha b_t^\theta \implies$ special case on next slide for intuition

Special case – just for intuition

- Let $\theta = 1 \Rightarrow \frac{dc^k}{c^k} = \frac{dc^p}{c^p}$ and evaluate at $\tilde{v}(c_t^k) = v(c_t^p, \dots) = v(c_t)$

$$\begin{aligned} \Rightarrow g_{\lambda_t} = & \frac{dc_t}{c_t} + \frac{N_t^p + N_t^k}{N_t^p + 2N_t^k} \cdot v(c_t) \cdot \frac{dN_t}{N_t} && \text{Base terms} \\ & + \frac{N_t^p}{N_t^p + 2N_t^k} \cdot \frac{u_{lt}l_t}{u_{ct}c_t} \cdot \frac{dl_t}{l_t} && \text{Leisure} \\ & + \frac{N_t^p}{N_t^p + 2N_t^k} \cdot \frac{u_{bt}b_t}{u_{ct}c_t} \cdot \frac{db_t}{b_t} && \text{Quantity of kids} \\ & + \frac{N_t^p}{N_t^p + 2N_t^k} \cdot \frac{u_{h^k_t}h_t^k}{u_{ct}c_t} \cdot \frac{dh_t^k}{h_t^k} && \text{Quality of kids} \end{aligned}$$

Double counting kids' consumption downweights all non-consumption terms

Implementing the generalized growth accounting

- Parents' FOCs maps *relative* weights in growth accounting to observables
 - l_t : $\frac{u_{lt}l_t}{u_{ct}c_t} = \frac{w_t h_t l_t}{c_t}$
 - b_t : $\frac{u_{bt}b_t}{u_{ct}c_t} = \frac{N_t^k}{N_t^p} \frac{(c_t^k + w_t h_t e_t)}{c_t}$
 - h_t^k : $\frac{u_{h^k t} h_t^k}{u_{ct} c_t} = \frac{N_t^k}{N_t^p} \frac{1}{\eta_t} \frac{w_t h_t e_t}{c_t}$, where: $\eta_t = \frac{f'(h_t e_t) h_t e_t}{f(h_t e_t)}$
- Calibrating η
 - Set $\eta = 0.24$
 - Sum of Mincer coefficients for parents' schooling, relative to own, for kids' wage (= .0142/.0591, Lee, Roys, Seshadri, 2014)
 - Choose e_t generously (all childcare) and $\frac{dh_t^k}{h_t^k}$ generously (half wage growth from H) \implies generous quality growth

Kids' vs. Parents' Consumption and the Value of Life

- Calibrating α and θ for $\frac{c_t^k}{c_t} = \alpha b^\theta$
 - USDA (2012) study: spending on kids vs. parents, 2-parent households
 - Spending with 2 kids ($b = 1$) gives $\alpha = 2/3$
 - Across 1, 2, or 3 kids suggests $\theta \approx 0.8$ (also consider $\theta = .6$ and $\theta = 1$)
- Calibrate value of year of life as same for child and adult in U.S. in 2006
 - Given preferences, implies equal utility flows at that time in U.S.
 - Consider robustness to $\frac{\tilde{v}(c_t^k)}{v(c_t, \dots)} = 0.8$ or 1.2
 - Allow $v(c_t, \dots)$ and $\tilde{v}(c_t^k)$ to evolve over time

Data to implement generalized growth accounting

- To implement calculation need series for:
 - # Children = 0-19 years old
 - # Adults = 20+ years old
 - $b_t = \text{Children} / \text{Adults}$
 - $l_{ct} = \text{paid work}$
 - $b_t e_t = \text{total child care}$
 - $l_t = 16 \text{ hrs} - l_{ct} - b_t \cdot e_t$
- Childcare from time use is main data constraint, restrict to 6 countries:
 - US (2003–2019)
 - Netherlands (1975–2006)
 - Japan (1991–2016)
 - South Korea (1999–2019)
 - Mexico (2006–2019)
 - South Africa (2000–2010)
- Additional data sources: PWT for per capita consumption and average market hours worked for ages 20-64, World Bank for population by age group

CEW Growth: Macro vs Micro

	MACRO			MICRO					
	CEW growth	pop term	cons term	CEW growth	pop term	cons term	leisure term	quality term	quantity term
USA	5.4	3.9	1.5	4.8	3.2	1.5	0.1	0.2	-0.3
NLD	4.5	2.5	2.1	4.0	2.0	2.1	0	0.4	-0.4
JPN	2.3	0.4	1.9	1.8	0.1	1.9	0	0.2	-0.4
KOR	4.4	1.7	2.6	3.7	0.9	2.6	0.6	0.4	-0.8
MEX	6.5	4.9	1.6	3.8	3.3	1.6	-0.3	0.1	-0.8
ZAF	6.8	4.3	2.6	5.9	3.1	2.6	1	0.3	-1

Share of population in CEW growth: Macro vs Micro

	MACRO	MICRO				
		Baseline	Robustness			
			Larger θ	Smaller θ	Larger v_k	Smaller v_k
USA	72%	68%	69%	66%	68%	67%
NLD	54%	50%	52%	48%	49%	52%
JPN	16%	5%	8%	3%	-9%	16%
KOR	40%	24%	27%	21%	15%	32%
MEX	76%	88%	90%	85%	87%	88%
ZAF	63%	53%	55%	51%	51%	55%

Tentative Conclusions

- Population growth contributes 1/2 to 2/3 of growth in country welfare
 - Complementary perspective to per capita consumption growth
- Because consumption runs into diminishing returns, each additional point of population growth is worth ...
 - 5pp of consumption growth in rich countries today
 - an average of 2.7pp for the world as a whole
- Results are robust to adjusting for migration and incorporating parent utility from children and privately optimal fertility choices

Other factors in welfare

- Changing inequality
 - Much of change *across countries*—estimates capture that
 - Ignores changes within countries
 - from Jones and Klenow (2016) those effects are small compared to factors here
- Changing population density
 - Density presumably increasing faster where faster population growth
 - But hedonic regressions for real wages across locations typically find density a positive amenity
 - See Ahlfeldt and Pietrostefani (2019) for literature review